#### HELMHOLTZ MUNICI

## What's in a Graph?

Bastian Rieck (@Pseudomanifold)

## Invocation



What's in a name? That which we call a rose By any other name would smell as sweet

(Romeo and Juliet, Act II, Scene II)



## Invocation



#### What's in a name? That which we call a rose By any other name would smell as sweet

(Romeo and Juliet, Act II, Scene II)



#### What's in a graph? That which we call our data By any other means would train as well



# What is a graph?

A graph is a tuple (V, E), consisting of a set of vertices V and a set of edges E, consisting of subsets of paired vertices.

# What is a graph?

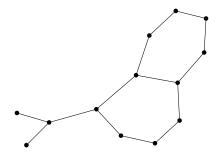
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If E is ordered instead, the graph is called directed.

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A graph is a triangulation of a manifold.



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A graph is a 1-dimensional simplicial complex.

A graph is a metric space.

A graph is a set system.

A collection of different attitudes

Alignment Belief





A collection of different attitudes

#### Alignment Belief

**Lawful** Graphs occur only in graph theory.





X

A collection of different attitudes

Alignment	Belief
Lawful	Graphs occur only in graph theory.
Neutral	Graphs can arise from other data modalities.

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Chaotic	Everything is a graph.	

J.

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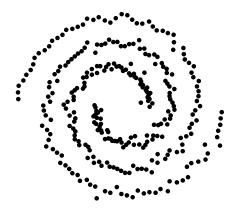
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Most graph theorists will agree that among the vast number of graphs that exist there are only a few thousand that can be considered really interesting.

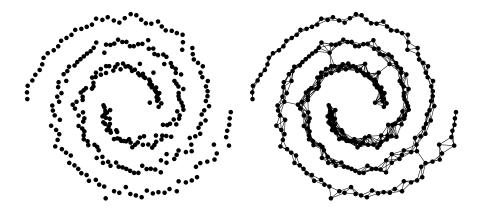
(https://houseofgraphs.org)



Point clouds



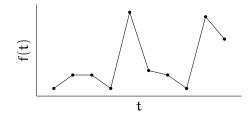
Point clouds



#### Rips graph at scale $\varepsilon$

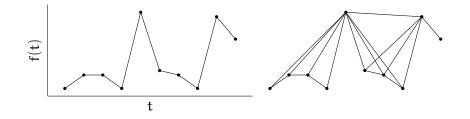
$$\mathfrak{R}_{\varepsilon} := (X, E)$$
 with  $E := \{x, y \in X \mid d(x, y) \leqslant \varepsilon\}$ 

Time series



<sup>1</sup>L. Lacasa, B. Luque, F. Ballesteros, J. Luque and J. C. Nuño, 'From time series to complex networks: The visibility graph', *Proceedings of the National Academy of Sciences* 105.13, 2008, pp. 4972–4975.

Time series



#### Visibility graph<sup>1</sup>

Connect observations  $(t_i, f_i)$  and  $(t_{i+1}, f_{i+1})$  if no other observations occur along their linear interpolation.

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Some are born geometrical, some achieve geometry, and some have geometry thrust upon them.





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We are not equipped to ask what it means to study a specific graph. We need to develop a (better) language for describing graph data. By treating all graphs the same, we are making a mistake.

# Does Topology Help in Graph Learning?

# Hypothesis

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Thus, making models aware of such features is bound to improve predictive performance.



**B. Rieck**\*, C. Bock\* and K. Borgwardt, 'A Persistent Weisfeiler–Lehman Procedure for Graph Classification', *Proceedings of the 36th International Conference on Machine Learning (ICML)*, 2019, pp. 5448–5458

Make Weisfeiler–Le(h)man aware of connected components and cycles.

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Method	Data set	
	MUTAG	PTC-MM
VH	85.96±0.27	$66.96 \pm 0.51$
EH	$85.69 \pm 0.46$	$61.61 \pm 0.00$
WL	$87.26 \pm 1.42$	$67.28 \pm 0.97$
P-WL P-WL-C	86.10±1.37 <b>90.51±1.34</b>	68.40±1.17 68.57±1.76

# Making graph neural networks topology-aware

M. Horn\*, E. De Brouwer\*, M. Moor, Y. Moreau, **B. Rieck**<sup>†</sup> and K. Borgwardt<sup>†</sup>, 'Topological Graph Neural Networks', *International Conference on Learning Representations (ICLR)*, 2022, arXiv: 2102.07835 [cs.LG]

Providing a new layer for use in graph neural networks.



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Providing a new layer for use in graph neural networks. Create new synthetic data sets with pronounced topological features. Getting high predictive performance on these data sets. Getting mediocre performance on other benchmark data sets. Getting better performance if node features are randomised.

On data sets with pronounced topological structures, we found that our method helps GNNs obtain substantial gains in predictive performance.



# Does Topology Help in Graph Learning? *It depends*.

Make your baseline as strong as possible.



Make your baseline as strong as possible. Iterate quickly to check your hypotheses.



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Iterate quickly to check your hypotheses.

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Use repeated nested cross-validation for small data sets.

L. O'Bray\*, **B. Rieck**\* and K. Borgwardt, 'Filtration Curves for Graph Representation', *Proceedings of the 27th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining (KDD)*, 2021, pp. 1267–1275:

For example, [our] previous work had results as high as 80% on IMDB-BINARY when considering just a single run of 10-fold cross validation. However, the results were not reflective of performance when repeated 10 times, which reduced [performance] to around 73%.



# **Troubling Trends**

K. Borgwardt, E. Ghisu, F. Llinares-López, L. O'Bray and **B. Rieck**, 'Graph Kernels: State-of-the-Art and Future Challenges', *Foundations and Trends*<sup>®</sup> in Machine Learning 13.5–6, 2020, pp. 531–712, arXiv: 2011.03854 [cs.LG]

We analysed the performance of graph kernels on benchmark data sets.

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Not using any deeper insights into graph structure here.

Data set	VH	EH
AIDS	$99.70 \pm 0.00$	$99.28 \pm 0.07$
DD	$68.68 \pm 3.04$	$78.52 \pm 0.34$
IMDB-BINARY	$50.58 \pm 0.20$	$73.46 \pm 0.60$
MUTAG	$85.98 \pm 0.40$	85.14±1.03
Mutagenicity	$67.01 \pm 0.83$	$49.13 \pm 1.75$
NCI1	64.66±0.53	$51.71 \pm 1.45$
NCI109	$63.24 \pm 0.54$	$51.45 \pm 2.06$
REDDIT-BINARY	$50.03 \pm 2.24$	$78.94 \pm 0.60$
SYNTHETICnew	$62.30 \pm 0.55$	$71.20 \pm 1.69$



C. Cai and Y. Wang, 'A simple yet effective baseline for non-attributed graph classification', 2018, arXiv: 1811.03508 [cs.LG]

Use a *local degree profile* to classify graphs, then train an SVM on the resulting features.

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In general, while not addressed in this paper, we note that understanding the power and limitation of various graph representations, [...] is crucial [...] and remains largely open.



## Is this graph the *right* graph?

X

J. Gasteiger, S. Weißenberger and S. Günnemann, 'Diffusion Improves Graph Learning', Advances in Neural Information Processing Systems, vol. 32, Curran Associates, Inc., 2019:

Edges in real graphs are often noisy or defined using an arbitrary threshold, so we can clearly improve upon this approach.

J. Topping, F. Di Giovanni, B. P. Chamberlain, X. Dong and M. M. Bronstein, 'Understanding over-squashing and bottlenecks on graphs via curvature', *International Conference on Learning Representations*, 2022:

More recently, there is a trend to decouple the input graph from the graph used for information propagation.

#### Question

Is the graph structure not necessary and we could equally well solve everything with a properly-regularised transformer-like architecture?

## A Closer Look At Our Data

#### Our data sets are not necessarily representative

J. Palowitch, A. Tsitsulin, B. Mayer and B. Perozzi, 'GraphWorld: Fake Graphs Bring Real Insights for GNNs', Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery & Data Mining (KDD), 2022, pp. 3691–3701

Oh, God, I could be bounded in a nutshell and count myself a king of infinite space, were it not that I have bad dreams. (Hamlet, Act II, Scene II)



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Our first finding is that standard benchmark graphs [...] cover only a small region of this graph space that GraphWorld is able to cover via synthetic graph generation.

And some things that should not have been forgotten were lost. History became legend. Legend became myth. (The Lord of the Rings)



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Typically, no provenance information of (benchmark) data sets.



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Typically, no *provenance* information of (benchmark) data sets. Typically, no *version* information.



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Typically, no provenance information of (benchmark) data sets.

Typically, no version information.

Often, no pre-defined splits.



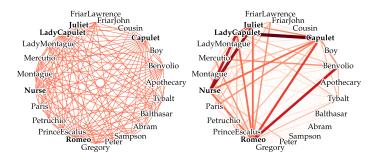
C. Coupette, J. Vreeken and **B. Rieck**, 'All the World's a (Hyper)Graph: A Data Drama', 2022, arXiv: 2206.08225 [cs.LG], URL: https://hyperbard.net



Three *valid* co-occurrence networks of characters in Shakespeare's Romeo and Juliet. Characters in Act III, Scene V are highlighted.



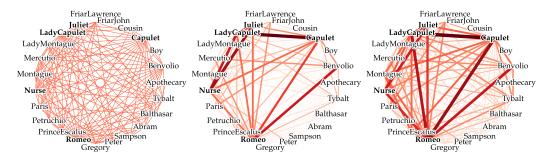
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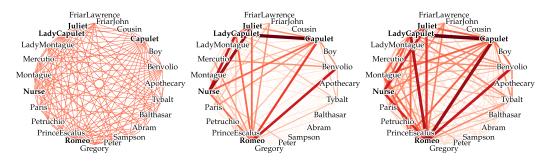
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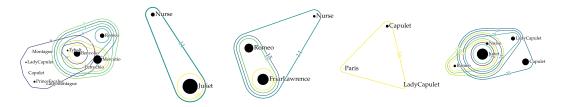
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#### Observation

Romeo and the Capulets almost never interact directly; our *modelling decision* introduces new information!

#### **Alternative models**

Hypergraphs



Modelling individual scenes of Act III of Romeo and Juliet provides a better overview of how all characters interact on stage.



pytorch-geometric

**Disclaimer**: The PyG team is doing an excellent job! This is *not* to be construed as a criticism of their work. We, as a community, should do more to support such endeavours!

```
$ rg -t py "^\s*url =" \
| grep -Eo "(http|https)://[a-zA-Z0-9./?=_%:-]*" \
| sort |
uniq -c
```

#### Hosts for data sets

Host	Count
ucl.ac.uk	1
is.tue.mpg.de	3
docs.google.com	7
drive.google.com	7
dropbox.com	/



pytorch-geometric, continued

Some additional data sets are also accessed via GitHub repositories, owned by private individuals or organisations:

abojchevski, flyingdoog, gasteigerjo, graphdml-uiuc-jlu, nd7141, INK-USC, kimiyoung, klicperajo, pmernyei, samihaija, shchur, steveazzolin, villmow, yandex-research, Yannick-S



pytorch-geometric, continued

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At present, no versioning or fingerprinting mechanism appears to be in place.

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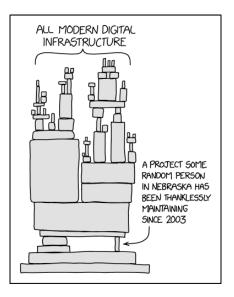
#### Some issues

At present, no versioning or fingerprinting mechanism appears to be in place. What happens if a repository is deleted? What happens if files are being changed? Is everyone training on the same data?



#### Is this the state of our data sets?

https://xkcd.com/2347/





## Is this where we are heading?

B. Haibe-Kains et al., 'Transparency and reproducibility in artificial intelligence', Nature 586.7829, 2020, E14–E16

#### **Matters** arising

## Transparency and reproducibility in artificial intelligence

https://doi.org/10.1038/s41586-020-2766-y	Benjamin Haibe-Kains <sup>12,3,4,5 ®</sup> , George Alexandru Adam <sup>3,5</sup> , Ahmed Hosny <sup>6,7</sup> ,
Received: 1February 2020	Farnoosh Khodakarami <sup>12</sup> , Massive Analysis Quality Control (MAQC) Society Board of Directors*, Levi Waldron <sup>8</sup> , Bo Wang <sup>2,3,5,30</sup> , Chris McIntosh <sup>2,4,5</sup> , Anna Goldenberg <sup>3,5,112</sup> , Anshul Kundaje <sup>3,5,4</sup> , Casey S. Greene <sup>5,5,8</sup> , Tamara Broderick <sup>70</sup> , Michael M. Hoffman <sup>12,3,5</sup> , Jeffrey T. Leek <sup>8</sup> , Keegan Korthauer <sup>9,28</sup> , Wolfgang Huber <sup>1</sup> , Alvis Brazma <sup>22</sup> , Joelle Pineau <sup>22,24</sup> , Robert Tibshiran <sup>25,47</sup> , Frov Hastie <sup>23,26</sup> , John P. A. Ioannidis <sup>25,3,27,22,29</sup> , John Quackenbush <sup>90,3,127</sup> & Hugo J. W. L. Aerts <sup>6,23,334</sup>
Accepted: 10 August 20 20	
Published online: 14 October 20 20	
Check for updates	

ar ising from S. M. McKinney et al. Nature https://doi.org/10.1038/s41586-019-1799-6 (2020)



Improving the Field

Keeping track of the provenance of data sets.

<sup>2</sup>T. Gebru et al., 'Datasheets for Datasets', Communications of the ACM 64.12, 2021, pp. 86–92.

Keeping track of the provenance of data sets. Fingerprinting of data sets (SHA-256).

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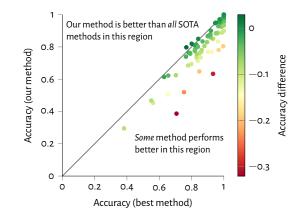
Keeping track of the provenance of data sets. Fingerprinting of data sets (SHA-256). Versioning data sets.

Using datasheets to describe graph data sets.<sup>2</sup>

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#### **Reporting results**

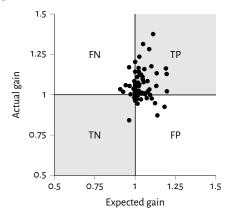
Learning from time series classification in data mining: run comparisons on as many data sets as possible, always comparing with the best available method.



Comparison of the predictive accuracy of our method against the respective state-of-the-art method for the 'UCR Time Series Archive' data sets.

### **Reporting results**

Learning from time series classification in data mining: calculate 'Texas Sharpshooter' plots, using a well-established algorithm as a baseline.<sup>3</sup>



A 'Texas Sharpshooter' plot, comparing *expected* gains (measured by comparing training performance) of our method with *actual* gains (measured by comparing test performance), relative to 1-DTW-KNN.

<sup>3</sup>G. E. A. P. A. Batista, E. J. Keogh, O. M. Tataw and V. M. A. de Souza, 'CID: an efficient complexity-invariant distance

#### Ending on a good note

Our problems are less of a technological and more of a social nature!

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Our problems are less of a technological and more of a social nature! We can fix them together.

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#### Acknowledgements

A lot of people helped shaped the opinions presented in this talk. Thank you to all of them!



Image sources: xkcd.com; Gerard Girbes Berges (The Noun Project)

